

14.3 Mechanical Advantage and Efficiency

A nutcracker is a machine that converts the input force applied to it into a larger force capable of cracking a nut.

Because it increases force, the nutcracker has a mechanical advantage greater than 1.



Mechanical Advantage



How does the actual mechanical advantage of a machine compare to its ideal mechanical advantage?

The **mechanical advantage** of a machine is the number of times that the machine increases an input force.



Because friction is always present, the actual mechanical advantage of a machine is always less than the ideal mechanical advantage.

Mechanical Advantage

Actual Mechanical Advantage

The mechanical advantage determined by measuring the actual forces acting on a machine is the actual mechanical advantage.

The **actual mechanical advantage** (AMA) equals the ratio of the output force to the input force.

Mechanical Advantage

A loading ramp is a machine used to move heavy items into a truck.

The mechanical advantage of a ramp with a rough surface is less than that of a similar smooth ramp because a greater force is needed to overcome friction.

Actual Mechanical Advantage

$$\text{Actual mechanical advantage} = \frac{\text{Output force}}{\text{Input force}}$$

Mechanical Advantage

Ideal Mechanical Advantage

The **ideal mechanical advantage** (IMA) of a machine is the mechanical advantage in the absence of friction.

Because friction reduces mechanical advantage, engineers often design machines that use low-friction materials and lubricants.

Calculating Mechanical Advantage

Ideal Mechanical Advantage

$$\text{Ideal mechanical advantage} = \frac{\text{Input distance}}{\text{Output distance}}$$

Calculating Mechanical Advantage

Math Practice

1. A student working in a grocery store after school pushes several grocery carts together along a ramp. The ramp is 3 meters long and rises 0.5 meter. What is the ideal mechanical advantage of the ramp?

Calculating Mechanical Advantage

Math Practice

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Answer:

$\text{IMA} = \text{Input distance} / \text{Output distance}$

$\text{IMA} = 3 \text{ m} / 0.5 \text{ m} = 6$

Calculating Mechanical Advantage

Math Practice

2. A construction worker moves a crowbar through a distance of 0.50 m to lift a load 0.05 m off of the ground. What is the IMA of the crowbar?

Calculating Mechanical Advantage

Math Practice

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Answer:

$\text{IMA} = \text{Input distance} / \text{Output distance}$

$\text{IMA} = 0.5 \text{ m} / 0.05 \text{ m} = 10$

Calculating Mechanical Advantage

Math Practice

3. The IMA of a simple machine is 2.5. If the output distance of the machine is 1.0 m, what is the input distance?

Calculating Mechanical Advantage

Math Practice

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Answer:

$$\text{Input distance} = (\text{IMA})(\text{Output distance})$$

$$\text{Input distance} = (2.5)(1.0 \text{ m}) = 2.5 \text{ m}$$

Efficiency



Why is the efficiency of a machine always less than 100 percent?

The percentage of the work input that becomes work output is the **efficiency** of a machine.



Because there is always some friction, the efficiency of any machine is always less than 100 percent.

Efficiency

Efficiency is usually expressed as a percentage.

Efficiency

$$\text{Efficiency} = \frac{\text{Work output}}{\text{Work input}} \times 100\%$$

For example, if the efficiency of a machine is 75 percent, then you know that 75 percent of the work input becomes work output.

Efficiency

If a machine requires 10.0 J of work input to operate, then the work output is 75% of 10.0 J.

$$\text{Work output} = \frac{\text{Work input} \times \text{Efficiency}}{100\%}$$

$$\text{Work output} = \frac{10.0 \text{ J} \times 75\%}{100\%} = 7.5 \text{ J}$$

Assessment Questions

1. Which statement about the actual mechanical advantage of a machine is true?
 - a. The actual mechanical advantage is greater than one if the input force is greater than the output force.
 - b. The actual mechanical advantage of a machine is greater than its ideal mechanical advantage when the output force is greater than the input force.
 - c. The actual mechanical advantage of a machine is always less than its ideal mechanical advantage.
 - d. The actual mechanical advantage of a machine is never affected by friction.

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ANS: C

Assessment Questions

2. If a lever raises a large rock 0.1 meters when the other end of the lever moves downward 2 meters, what is the ideal mechanical advantage of the lever?
- a. 0.05
 - b. 0.5
 - c. 2
 - d. 20

Assessment Questions

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ANS: D

Assessment Questions

3. A machine is used to accomplish 300 J of work. If the efficiency of the machine is 60 percent, what is the necessary work input?
- a. 180 J
 - b. 360 J
 - c. 500 J
 - d. 750 J

Assessment Questions

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ANS: A

Assessment Questions

1. The efficiency of any machine is less than 100% because of losses due to friction.

True

False

Assessment Questions

1. The efficiency of any machine is less than 100% because of losses due to friction.

True

False

ANS: T